

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS
General Certificate of Education
Advanced Subsidiary Level and Advanced Level

## MATHEMATICS

9709/06
Paper 6 Probability \& Statistics 1 (S1)

## READ THESE INSTRUCTIONS FIRST

If you have been given an Answer Booklet, follow the instructions on the front cover of the Booklet.
Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use a soft pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.
Answer all the questions.
Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.
The use of an electronic calculator is expected, where appropriate.
You are reminded of the need for clear presentation in your answers.
At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.
The total number of marks for this paper is 50 .
Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.

1 The length of time, $t$ minutes, taken to do the crossword in a certain newspaper was observed on 12 occasions. The results are summarised below.

$$
\Sigma(t-35)=-15 \quad \Sigma(t-35)^{2}=82.23
$$

Calculate the mean and standard deviation of these times taken to do the crossword.

2 Jamie is equally likely to attend or not to attend a training session before a football match. If he attends, he is certain to be chosen for the team which plays in the match. If he does not attend, there is a probability of 0.6 that he is chosen for the team.
(i) Find the probability that Jamie is chosen for the team.
(ii) Find the conditional probability that Jamie attended the training session, given that he was chosen for the team.

3 (a) The random variable $X$ is normally distributed. The mean is twice the standard deviation. It is given that $\mathrm{P}(X>5.2)=0.9$. Find the standard deviation.
(b) A normal distribution has mean $\mu$ and standard deviation $\sigma$. If 800 observations are taken from this distribution, how many would you expect to be between $\mu-\sigma$ and $\mu+\sigma$ ?

4 The lengths of time in minutes to swim a certain distance by the members of a class of twelve 9 -year-olds and by the members of a class of eight 16 -year-olds are shown below.

| 9-year-olds: | 13.0 | 16.1 | 16.0 | 14.4 | 15.9 | 15.1 | 14.2 | 13.7 | 16.7 | 16.4 | 15.0 | 13.2 |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 16-year-olds: | 14.8 | 13.0 | 11.4 | 11.7 | 16.5 | 13.7 | 12.8 | 12.9 |  |  |  |  |

(i) Draw a back-to-back stem-and-leaf diagram to represent the information above.
(ii) A new pupil joined the 16-year-old class and swam the distance. The mean time for the class of nine pupils was now 13.6 minutes. Find the new pupil's time to swim the distance.

5
(i) Find the number of ways in which all twelve letters of the word REFRIGERATOR can be arranged
(a) if there are no restrictions,
(b) if the Rs must all be together.
(ii) How many different selections of four letters from the twelve letters of the word REFRIGERATOR contain no Rs and two Es?

6 The probability that New Year's Day is on a Saturday in a randomly chosen year is $\frac{1}{7}$.
(i) 15 years are chosen randomly. Find the probability that at least 3 of these years have New Year's Day on a Saturday.
(ii) 56 years are chosen randomly. Use a suitable approximation to find the probability that more than 7 of these years have New Year's Day on a Saturday.

7 A vegetable basket contains 12 peppers, of which 3 are red, 4 are green and 5 are yellow. Three peppers are taken, at random and without replacement, from the basket.
(i) Find the probability that the three peppers are all different colours.
(ii) Show that the probability that exactly 2 of the peppers taken are green is $\frac{12}{55}$.
(iii) The number of green peppers taken is denoted by the discrete random variable $X$. Draw up a probability distribution table for $X$.

BLANK PAGE

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

University of Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.

